

Name _____

Period of a Pendulum

1. Measure the total time for a $m = 0.05$ kg, $L = 75$ cm, $A \approx 30^\circ$ (the angle between 4:00 and 6:00), pendulum to make 20 oscillations. (First set the pendulum *already* swinging; then start timing and start counting with "0" instead of "1" the moment the pendulum has swung all the way back.) Then divide by 20 to determine the period T (in seconds) of this pendulum.
2. Experimentally determine the dependence of the period T on the parameters below. (i) Record each new period, and (ii) state whether the period T depends (\uparrow , \downarrow , or constant) on the following parameters:
 - (a) Mass $m \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (b) Mass $m \downarrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (c) String length $L \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (d) String length $L \downarrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (e) Oscillation amplitude $A \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (f) Oscillation amplitude $A \downarrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (g) Gravitational constant $g \downarrow$ (?) (T \uparrow , \downarrow , or constant?)
 - (h) Constant phase $\phi \downarrow \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)

The exact expression for a pendulum period is $T =$ _____.



- Look for *significant* dependencies, and not negligible variations.
- Change one parameter at a time!

Mass-Spring Period

1. Measure the total time for a $m = 0.5$ kg, $k \approx 9.5$ N/m, $A = 5$ cm (as measured down from its equilibrium position) to make 20 oscillations. (First set the mass *already* oscillating; then start timing and start counting with "0" instead of "1" the moment the mass is at its lowest point.) Then divide by 20 to determine the period T (in seconds) of this mass-spring system.
2. Experimentally determine the dependence of the period T on the parameters below. (i) Record each new period, and (ii) state whether the period T depends (\uparrow , \downarrow , or constant) on the following parameters:
 - (a) Mass $m \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (b) Mass $m \downarrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (c) Spring strength $k \uparrow$ T _____ s
(use two springs in parallel) (T \uparrow , \downarrow , or constant?)
 - (d) Spring strength $k \downarrow$ T _____ s
(use two springs in series) (T \uparrow , \downarrow , or constant?)
 - (e) Oscillation amplitude $A \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (f) Oscillation amplitude $A \downarrow$. T _____ s (T \uparrow , \downarrow , or constant?)
 - (g) Constant phase $\phi \downarrow \uparrow$. T _____ s (T \uparrow , \downarrow , or constant?)

The exact expression for a mass-spring period is $T = \underline{\hspace{2cm}}$.

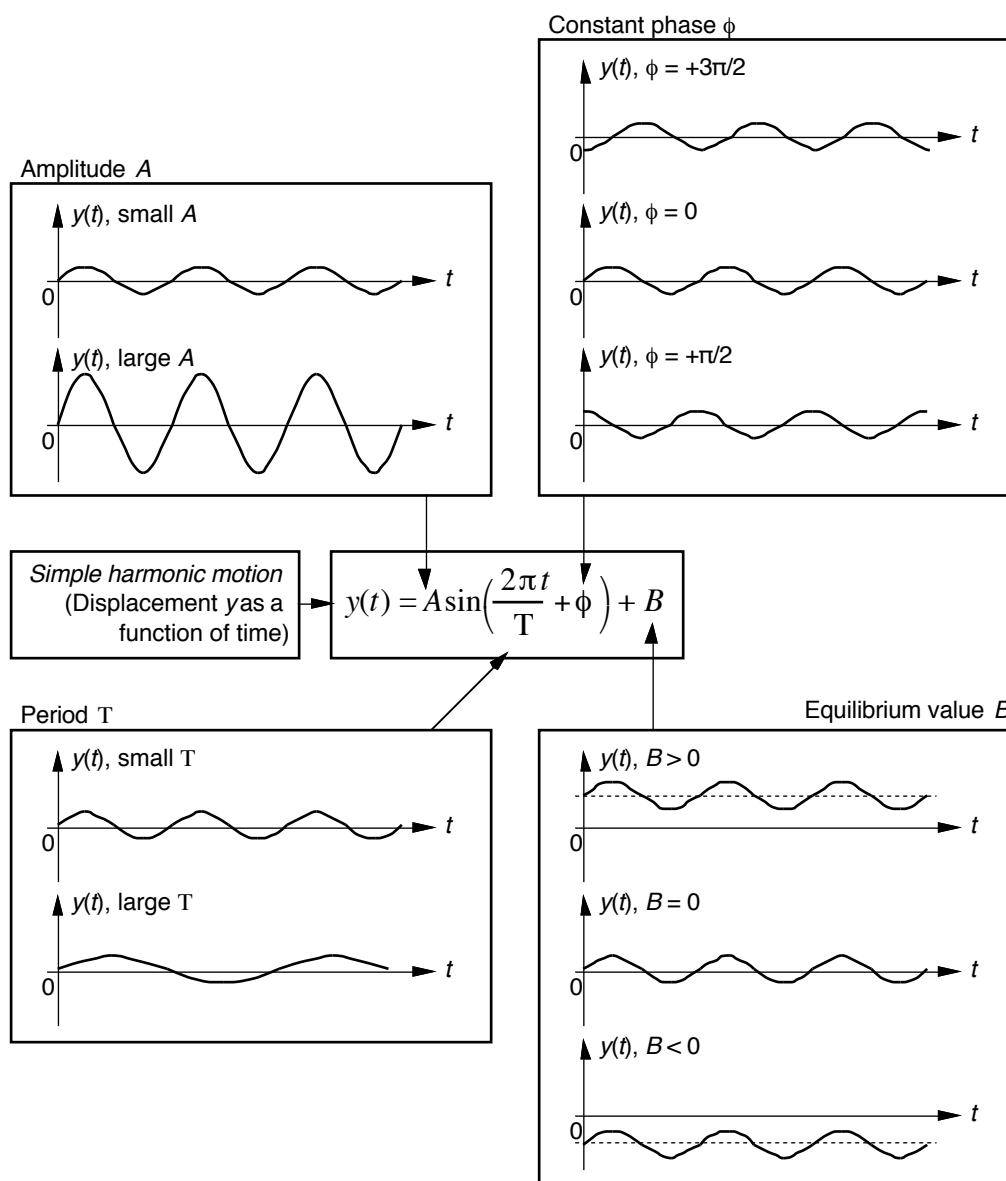


- Look for *significant* dependencies, and not negligible variations.
- Change one parameter at a time!

Simple Harmonic Motion (SHM) parameters

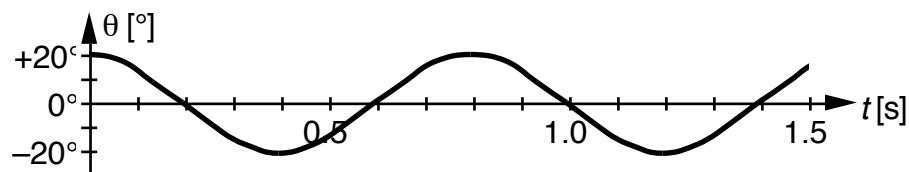
The most general form of the equation that describes *any* object undergoing SHM (simple harmonic motion) is given by:

$$y(t) = A \sin\left(\frac{2\pi t}{T} + \phi\right) + B.$$



Applying SHM Parameters

Consider the specific case of this graph of angular position versus time for an $m = 0.2$ kg pendulum:

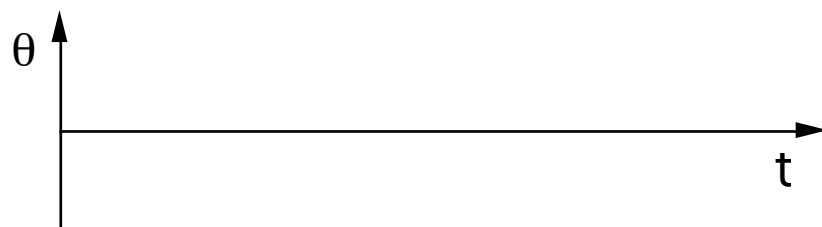


1. What are the values *and* units of these SHM parameters?

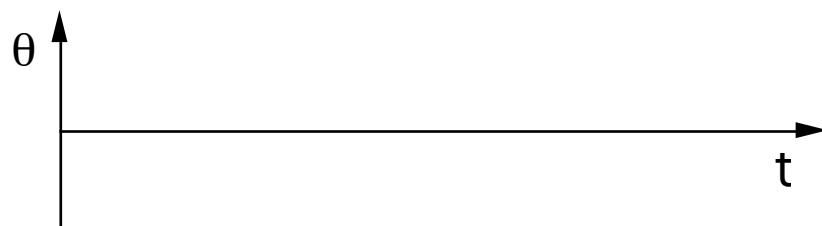
	Value?	Units?
(a) A		
(b) T		
(c) ϕ		
(d) B		

For the following situations (2)-(5), redraw the angular position $\theta(t) \leftrightarrow y(t)$ versus time graph from (1) if the physical parameters below are changed. Scale (rescale) your axes as necessary.

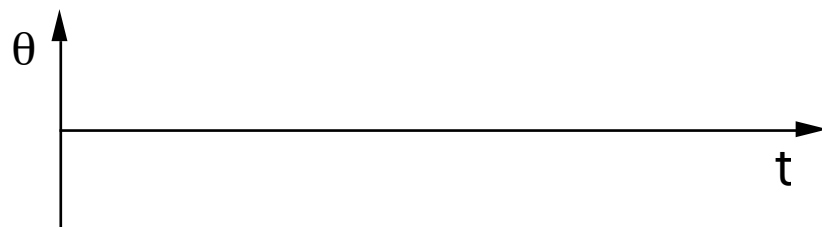
- The mass m is doubled.
- The string L is doubled.
- The amplitude A is doubled.
- The parameter ϕ is doubled.
- For each of the above situations (2)-(5), demonstrate for yourselves what the actual pendulum motion looks like, by using the appropriate m , L , A , and ϕ in your demonstration.



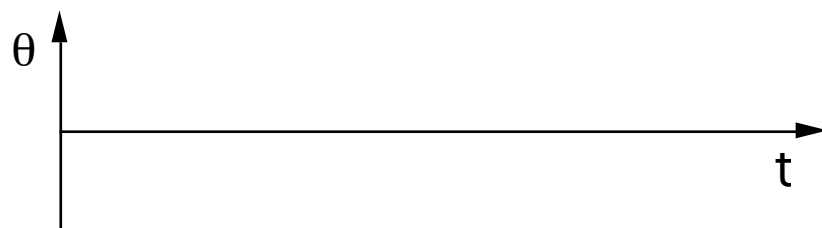
mass is doubled



string L is doubled



amplitude is doubled



ϕ is doubled